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# HYPERNUCLEAR MATTER CALCULATIONS

by

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Abstract: In this paper results are reported for the binding energy  $B_{\Lambda}$  of a  $\Lambda$ -particle in nuclear matter, obtained by means of the differential equation for the Jastrow  $\Lambda$ -nucleon correlation function f, using eentral potentials and values for the density of nuclear matter, which are smaller than the initially used (0.172 nucleons/fm<sup>3</sup>) and have been more recently determined. Results are also given by using the integrodifferential equation for the determination of f and various approximate expressions for the  $\Lambda$ -nucleon distribution function  $G_{N\Lambda}(r)$  and its functional derivative.

#### 1. INTRODUCTION

Considerable work has been done for the calculation of the binding energy of a  $\Lambda$ -particle in nuclear matter  $B_{\Lambda} = -E_{\Lambda}$ . Both reaction matrix and variational techniques have been employed and use of various potentials, mainly centrals, has been made<sup>1-7</sup>.

The possibility of obtaining the A-nucleon correlation function, in the variational approach, as a solution of a differential equation, which is derived by applying the variational principle to the first-order-energy expression,  $E_{\Lambda}^{(1)}$  has also been examined. Two ways of determining the parameter  $\beta$ , related to the Lagrange multiplier, which is due to the healing condition have been considered<sup>8</sup>. The results are improved with the second choice of  $\beta$ , which corresponds to the «better convergence» (BC choice) of the cluster expansion. There is, however, still considerable overbinding and it appears interesting to investigate possible other ways of obtaining reduced values of  $B_{\Lambda}$ . In this paper results are reported of calculations performed with smaller values of the density of nuclear matter  $\rho$ . It should be noted that the analyses of experiments of elastic proton scattering from nuclei, made by Greenless et al.<sup>10</sup> led to values of  $\rho$  smaller than the value of 0.172 nucleons/fm<sup>3</sup>, which has been more commonly used. In addition, results obtained by means of the integrodifferential equation for the  $\Lambda$ -nucleon correlation function, are given. In the next section the formalism is briefly described and in the final one the results are given and discussed.

# 2. THE FORMALISM

If the functional variation is performed to the first order energy functional  $E_A^{(i)}$ 

$$\mathbf{E}_{\mathbf{A}}^{(1)} = \rho \int \mathbf{f} (\mathbf{r}) \mathbf{H}_{\mathbf{A}\mathbf{i}} \mathbf{f}(\mathbf{r}) \vec{\mathrm{dr}}$$
(1)

with the healing condition

$$\rho \int (f(r) - 1)^2 \quad \vec{dr} = I_1 < \infty \tag{2}$$

the Euler equation for the A-nucleon correlation function is the following differential equation<sup>8</sup>

$$\frac{\mathrm{d}^{2}f_{0}}{\mathrm{d}r^{2}} + \frac{2}{r}\frac{\mathrm{d}f_{0}}{\mathrm{d}r} - \frac{2\mu_{AN}}{\hbar^{2}}V_{AN}(r) f_{0} -\beta^{2} f_{0} = -\beta^{3}, c \leq r < \infty$$
(3)

This is solved numerically with boundary conditions

$$f(c) = 0, f(\infty) = 1$$
 (4)

A few additional remarks concerning this approach are in order.

Firstly, we observe that a relation holds between  $E_{\Delta}^{(1)}$ ,  $I_1$  and the intergal  $I_2$ , defined by

$$I_{a} = \rho \int (f^{2} - 1) \vec{dr}$$
(5)

This relation is the following :

$$\mathbf{E}_{\Delta}^{(1)} = -\frac{\hbar^2}{4\mu_{\Delta N}} \beta^2 \left(\mathbf{I}_1 + \mathbf{I}_2\right) \tag{6}$$

By using the above expression we may avoid the numerical intergation of one of the integrals  $E_{A}^{(0)}$ ,  $I_{1}$  and  $I_{2}$ .

Secondly, in the case of the exponential with hard core potential, in which the derivation of an analytic solution is possible, we may find the asymptotic form of the solution for large internucleon distances or for large values of the parameter  $\beta$ . This asymptotic form is the following:

$$f(\mathbf{r}) \simeq 1 - \frac{1}{r} \left\{ c e^{-\beta (\mathbf{r} - c)} + \frac{2\mu_{\Delta N}}{\hbar^2} \frac{V_0}{\beta^2 - \mu^2} \left( c - \frac{2\mu}{\beta^2 - \mu^2} \right) e^{-\beta (\mathbf{r} - c)} - \frac{2\mu_{\Delta N}}{\hbar^2} \frac{V_0}{\beta^2 - \mu^2} \left( \mathbf{r} - \frac{2\mu}{\beta^2 - \mu^2} \right) e^{-\mu (\mathbf{r} - c)} \right\}$$
(7)

Furthermore, in the case of very large values of  $\beta$ , the following asymptotic expressions of  $E_{\Lambda}^{(1)}$ ,  $I_1$  and  $I_2$  may be derived:

$$E_{\Lambda,as}^{(j)}(\beta) = 4 \pi \rho \; \frac{\hbar^2}{2\mu_{\Lambda N}} \left[ \frac{1}{2} c^2 \beta + c - \frac{2\mu_{\Lambda N}}{\hbar^2} \; \frac{V_0}{\mu^3} \; (\mu^2 c^2 + 2\mu c + 2) \right] \; (8)$$

$$I_{1,as} = \frac{4}{3} \pi \rho c^{s} + \frac{2\pi \rho c^{2}}{\beta}$$

$$\tag{9}$$

and

$$I_{a,as} = -\frac{4}{3} \pi \rho c^{s} - \frac{6\pi \rho c^{2}}{\beta}$$
(10)

It is seen that  $E_{\Delta,as}^{(D)}$  is represented by a straight line while  $I_{1,as}$  and  $I_{2,as}$  by hyperbolas.

When the functional variation is applied to the expression of  $E_{A}$ :

$$E_{A} = 4\pi\rho \int_{0}^{\infty} d\mathbf{r} \cdot \mathbf{r}^{2} \left[ \mathbf{f} (\mathbf{r}) \mathbf{W} (\mathbf{r}) \mathbf{f} (\mathbf{r}) \right] \mathbf{G}_{\mathbf{N}A} (\mathbf{r})$$
(11)

with the conditions

$$4\pi\rho \int_{\infty}^{\infty} (f-1)^{2} G_{NA} (r) r^{2} dr = \tilde{I}_{1} < \infty$$
(12)

and

$$4\pi\rho \int_{0}^{\infty} (\tilde{f}^{2} G_{NA}(r) - 1) r^{2} dr = \tilde{I}_{2} < \infty$$
(13)

a complicated integrodifferential equation for f is obtained (see equ. 3.6 of ref. 11). The expressions of W and the distribution function  $G_{NA}(\mathbf{r})$  are also given in ref. 11.

The calculation of the functional derivative of  $G_{NA}$  which appears in the integrodifferential equation may be done by using the expression (3.3) of reference 11 and substituting subsequently an approximate expression for  $G_{NA}$ , as for example

$$G_{NA}(r) \simeq 1 + X_{(r)} \tag{14}$$

or, according to Westhaus⁵

$$G_{NA} \simeq e^{\chi(r)}$$
 (15)

where

$$X(\mathbf{r}) = \rho \int \vec{dr}_{1\Lambda} [f^2(\mathbf{r}_{1\Lambda}) - 1] [g_0^{(2)}(|\vec{r}_{1\Lambda} - \vec{r}|) - 1]$$
(16)

$$g_{0}^{(2)} (|\vec{r}_{1\Lambda} - \vec{r}|) = f^{2}_{NN} (|\vec{r}_{1\Lambda} - \vec{r}|) [1 - \frac{1}{4} l^{2} (k_{F} |\vec{r}_{1\Lambda} - \vec{r}|)], \quad l(x) = \frac{3j_{1}(x)}{x}$$
(17)

An alternative procedure is to calculate the functional derivative directly from expressions (14) or (15).

The following cases may therefore be considered in solving the integrodifferential equation:

$$A_{1}: \qquad G_{NA}(r) \simeq 1 + X(r) \tag{18}$$

$$\frac{\delta G_{NA}(\mathbf{r})}{\delta f(\mathbf{r}_{1A})} \simeq 2\rho f(\mathbf{r}_{1A}) \left[g_{0}^{(2)}(|\vec{\mathbf{r}}_{1A} - \vec{\mathbf{r}}|) - 1\right]$$
(19)

A<sub>a</sub>:  $G_{NA}(r) \simeq e^{\chi(r)}$ 

$$\frac{\delta G_{N\Lambda}(\mathbf{r})}{\delta f(\mathbf{r}_{1\Lambda})} \simeq 2\rho f(\mathbf{r}_{1\Lambda}) e^{\chi(\mathbf{r})} [g_{0}^{(2)}(\vec{\mathbf{r}_{1\Lambda}} - \vec{\mathbf{r}} |) - 1]$$
(21)

(20)

$$\mathbf{B}_{\mathbf{r}}: \qquad \mathbf{G}_{\mathbf{N}\mathbf{A}}(\mathbf{r}) \simeq \mathbf{1} + \mathbf{X}(\mathbf{r}) \tag{22}$$

$$\frac{\delta G_{\mathbf{N}\mathbf{A}}(\mathbf{r})}{\delta f(\mathbf{r}_{\mathbf{1}\mathbf{A}})} \simeq 2\rho f(\mathbf{r}_{\mathbf{1}\mathbf{A}}) \left[1 + X(\mathbf{r}_{\mathbf{1}\mathbf{A}})\right] \left[1 + X(\mathbf{r})\right] \left[g_{0}^{(2)}\left(\left|\vec{\mathbf{r}}_{\mathbf{1}\mathbf{A}} - \vec{\mathbf{r}}\right|\right) - 1\right] (23)$$

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and

B2:

$$G_{N_{\Lambda}}(\mathbf{r}) \simeq e^{\chi(\mathbf{r})}$$
 (24)

$$\frac{\delta G_{N\Lambda}(\mathbf{r})}{\delta f(\mathbf{r}_{1\Lambda})} \simeq 2\rho f(\mathbf{r}_{1\Lambda}) e^{\chi(\mathbf{r}_{1\Lambda})} e^{\chi(\mathbf{r})} \left[g_{0}^{(2)}\left(\overrightarrow{|\mathbf{r}_{1\Lambda} - \mathbf{r}|}\right) - 1\right]$$
(25)

From the examination of the integrodifferential equation at large distances it turns out that the Lagrange multiplier  $\lambda_1$  may be taken equal to zero. This value will be assumed in this paper.

# 3. RESULTS AND DISCUSSION

The results obtained with the differential equation for f are given first.

The potentials H, E' and B' of Herndon and Tang<sup>12 13</sup> were used and two values for the density of nuclear matter: a)  $\rho=0.166$  nucleons/ fm<sup>3</sup> (k<sub>F</sub>=1.35 fm<sup>-1</sup>) and b)  $\rho$ =0.121 nucleons/fm<sup>3</sup> (k<sub>F</sub>=1.2144 fm<sup>-1</sup>). For each value of the density the nucleon-nucleon correlation function was determined by using the potentials OMY-I (functions  $g'_2$  and  $g''_2$ ) and OMY-II14 (functions g' and g' respectively) described in ref. 9. The nucleon-nucleon correlation function has the form (44) of ref. (9) and the parameters are the following<sup>15</sup>.

For g'a:  $c_{NN} = 0.6 \text{ fm},$  $a = 2.3284 \text{ fm}^{-1}$ , b = 1.37282For g<sub>2</sub>  $c_{NN} = 0.6 \text{ fm},$  $a = 2.3791 \text{ fm}^{-1}$ , b = 1.3664For g's  $a = 2.5621 \text{ fm}^{-1}$ , b = 1.26792 $c_{NN} = 0.4 \text{ fm},$ and for g'  $c_{NN} = 0.4 \text{ fm},$  $a = 2.5964 \text{ fm}^{-1}$ , b = 1.24612

The parameter  $\beta$  was determined in two ways, as in ref. 9. The results for the various cases are given on tables I-VIII. It is seen that the values of  $B_A$  are closer to the empirical value compared to the corresponding ones of ref 9. In particular with the smaller value for the density and the potential B' the results are very good and in agreement with the empirical value.

The integrodifferential equation was solved numerically with the

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method of iteration. The correlation function  $f_0$ , together with the corresponding  $f_0$  which satisfies the differential equation is shown in fig.

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1 for the BC choice for  $\beta_1$  ( $\beta_1^2 = \frac{2\mu_{AN}}{\hbar^2} \lambda_2$ ) and potential B'. In fig. 2 the values of the healing integral are plotted as functions of  $\beta$  (or  $\beta_1$ ) and in fig. 3 the  $E_A^{(1)}$ ,  $E_A^{(2)}$  and their sum  $E_A$  are plotted as functions of  $\beta_1$ . It is seen from the latter figure that the minimum of  $E_A$  corresponds now to  $\beta_1 \rightarrow 0$ . This is well-understood since the minimum should appear when the integral constraint has the least possible effect.

The results obtained with the integrodifferential equation are shown in tables IX-XII. It is seen that with potential B' do not differ much from the results obtained with the differential equation, while with potential E' there is more deviation from the empirical value of  $E_{\Delta}$ . It is also seen that the results in cases  $B_{1}$  and  $B_{2}$  are very slightly better. The results for  $E_{\Delta}$  with the smaller value for the density  $\rho$  are closer to the empirical value as in the case of the differential equation. It should be finally noted that in the case of the integrodifferential equation the inaccuracies are larger and this should be kept in mind in the assessment of the results.

We would like to thank Mr. Panos for computational assistance and the staff of the computing centre of the University of Thessaloniki, where the computations were performed.

#### TABLE I.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ (ME choice). The g'<sub>2</sub> nucleon-nucleon correlation function and the value  $\varrho=0.166$ nucleons fm<sup>3</sup> for the density of nuclear matter were used.

Potential	E <sup>(1)</sup>	$E^{(2)}_{\Lambda}$	$E_{\Lambda} = E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$	Iı	$I_{\mathfrak{d}}$
	(MeV)	(MeV)	(MeV)		
H	-86.1	13.0	-73.1	0,259	1.164
$\mathbf{E'}$	-71.0	8.5	-62.5	0.140	1.209
B'	-49.4	4.4	-45.0	0.061	0590.

#### TABLE II.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ (ME choice). The  $g_3'$  nucleon-nucleon correlation function and the value  $\varrho=0.166$ nucleons/fm<sup>3</sup> for the density of nuclear matter were used.

Potential	${ m E}^{(1)}_{\Lambda}$ (MeV)	E <sup>(2)</sup> (MeV)	$\begin{array}{c} \mathrm{E}_{\Lambda} = \mathrm{E}_{\Lambda}^{(1)} + \mathrm{E}_{\Lambda}^{(2)} \\ (\mathrm{MeV}) \end{array}$	$\mathtt{I_1}$	$I_2$
H	-88.8	12.2	-76.6	0.286	1.780
$\mathbf{E}'$	-72.8	8.4	-64.4	0.160	1.784
$\mathbf{B}'$	-50.4	5.0	-45.4	0.072	1.274

### TABLE III.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $\left|E_{\Lambda}^{(2)} E_{\Lambda}^{(1)}\right|$ (BC choice). The  $g_2'$  nucleon-nucleon correlation function and the value  $\varrho=0.166$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used.

Potential	$E^{(1)}_{\Lambda}$	${\rm E}^{(2)}_{\Lambda}$	$\mathbf{E}_{\Lambda} = \mathbf{E}_{\Lambda}^{(1)} + \mathbf{E}_{\Lambda}^{(2)}$	$I_1$	$\mathbf{I}_{2}$
	(MeV)	(MeV)	(MeV)		
н	-76.0	7.8	-68.2	0.215	0.092
$\mathbf{E'}$	-61.9	4.2	-57.7	0.101	0.102
B'	-38.8	0.6	-38.2	0.030	0.013

#### TABLE IV.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $\left| E_{\Lambda}^{(2)} \right| \left| E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_3'$  nucleon-nucleon correlation function and the value  $\varrho=0.166$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used.

Potential	${\rm E}^{(1)}_{\Lambda}$	$E^{(2)}_{\Lambda}$	$E_{\Lambda} = E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$	$I_1$	$\mathbf{I}_{2}$
	(MeV)	(MeV)	(MeV)		
H	-75.4	5.2	-70.2	0.214	0.075
$\mathbf{E}'$	-61.8	3.2	-58.6	0.101	0.096
B'	-40.1	0.9	-39.2	0.030	0.022

#### TABLE V.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ (ME choice). The  $g_2^{\prime\prime}$  nucleon-nucleon correlation function and the value  $\varrho=0.121$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used.

Potential	$\mathbf{E}^{(1)}_{\mathbf{A}}$	$E^{(2)}_{\Lambda}$	$\mathbf{E}_{\Lambda} = \mathbf{E}_{\Lambda}^{(1)} + \mathbf{E}_{\Lambda}^{(2)}$	$I_1$	$I_2$
	(MeV)	(MeV)	$({ m MeV})$		
H	-64.7	9.0	-55.7	0.208	1.298
$\mathbf{E'}$	-53.1	6.1	-47.0	0.117	1.301
B'	-37.1	3.7	-33.4	0.058	1.092

### TABLE VI.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ (ME choice). The  $g_3''$  nucleon-nucleon correlation function and the value  $\varrho=0.121$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used.

Potential	$E^{(1)}_{\Lambda}$	E <sup>(2)</sup>	$\mathbf{E}_{\Lambda} = \mathbf{E}_{\Lambda}^{(1)} + \mathbf{E}_{\Lambda}^{(2)}$	Iı	Ia
	(MeV)	(MeV)	(MeV)		
Η	-66.5	8.8	~57.7	0.233	1.829
E'	-54.4	6.3	-48.1	0.138	1.840
B'	-37.6	3.9	-33.7	0.066	1.301

# TABLE VII.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $\left| E_{\Lambda}^{(2)} / E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_2^{"}$  nucleon-nucleon correlation function and the value  $\varrho=0.121$  nucleons fm<sup>3</sup> for the density of nuclear matter were used.

Potential	$E^{(1)}_{\Lambda}$	E <sup>(2)</sup>	$E_{\Lambda} = E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$	Iı	$I_2$
	(MeV)	(MeV)	(MeV)		
Ħ	-55.0	4.0	-51.0	0.156	0.054
$\mathbf{E}'$	-44.7	2.2	-42.5	0.073	0.063
$\mathbf{B}'$	-28.0	0.3	~27.7	0.022	0.008

# TABLE VIII.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(4)} + E_{\Lambda}^{(2)}$ ,  $I_1$  and  $I_2$  for values of  $\beta$  which minimize  $\left| E_{\Lambda}^{(2)} / E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_{3}^{"}$  nucleon-nucleon correlation function and the value  $\varrho=0.121$  nucleons fm<sup>3</sup> for the density of nuclear matter were used

Potential	$E^{(1)}_{\Lambda}$	${\rm E}^{(2)}_{\Lambda}$	$E_{\Lambda} = E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$	Iı	$I_2$
	(MeV)	(MeV)	(MeV)		
н	-54.3	2.6	-51.7	0.155	0.032
$\mathbf{E}'$	-44.3	1.6	~42.7	0.072	0.053
$\mathbf{B}'$	~28.9	0.5	-28.4	0.022	0.014







Fig. 2. The «healing integral»  $I_1$  as a function of  $\beta$  (or  $\beta_1$ ). (Nucleon-nucleon correlation function  $g_2$ , potential B',  $\varrho=0.172$  nucleons (fm<sup>3</sup>). The solid line corresponds to the  $I_1$  obtained by using the differential equation and the dashed line to the  $I_1$ obtained by using the integrodifferential one. The choice  $B_1$  for  $G_{N\Lambda}$  and  $\frac{\delta G_{N\Lambda}}{\delta f}$ was made.



Fig. 3. The first and second order energies and their sum as functions of  $\beta_1$ . (Nucleon-nucleon correlation function  $g_2$ , potential B' and  $\varrho=0.172$  nucleons  $fm^3$ ). The choice  $B_1$  for  $G_{N\Lambda}$  and  $\frac{\delta G_{N\Lambda}}{\delta f}$  was made.

# TABLE IX.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$  and  $I_1$  for values of  $\beta_1$  which minimize  $\left| E_{\Lambda}^{(2)} / E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_2$  nucleon-nucleon correlation function, the potential B' and the value  $\varrho=0.172$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used in solving the integrodifferential equation.

Case	$\mathbb{E}^{(1)}_{\Lambda}$	E <sup>(2)</sup>	$\mathrm{E}^{(1)}_{\mathrm{A}}\!\!+\!\mathrm{E}^{(2)}_{\mathrm{A}}$	$\mathrm{I_1}$
	(MeV)	(MeV)	(MeV)	
$A_1$	-40.6	0.7	-39.9	0.031
$A_2$	-40.4	0.7	-39.7	0.031
$\mathbb{B}_1$	~40.2	0.7	-39.5	0.031
$\mathbb{B}_2$	-40.2	0.7	-39.5	0.031

### TABLE X.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$  and  $I_{1}$  for values of  $\beta_{1}$  which minimize  $\left| E_{\Lambda}^{(2)} / E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_{2}$  nucleon-nucleon correlation function, the potential E' and the value  $\varrho=0.172$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used in solving the integrodifferential equation.

Case	$E^{(1)}_{\Lambda}$	Ε <sup>(2)</sup>	$\mathrm{E}^{(1)}_{\Lambda}\!\!+\!\mathrm{E}^{(2)}_{\Lambda}$	${\rm I}_{\bf 1}$
	(MeV)	(MeV)	(MeV)	
$A_1$	-68.3	4.7	-63.6	0.115
$A_2$	-67.8	5.1	-62.7	0.114
$\mathbb{B}_{1}$	-67.6	5.0	-62.6	0.113
$\mathbb{B}_2$	-67.5	5.1	-62.4	0.113

#### TABLE XI.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$  and  $I_1$  for values of  $\beta_1$  which minimize  $\left| E_{\Lambda}^{(2)} / E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_2'$  nucleon-nucleon correlation function, the potential B' and the value  $\varrho=0.166$  nucleons/fm<sup>2</sup> for the density of nuclear matter were used in solving the integrodifferential equation.

Case	E(1)	E <sup>(2)</sup>	$\mathrm{E}^{(1)}_{\Delta}\mathrm{+E}^{(2)}_{\Delta}$	$\mathbb{I}_{\mathtt{l}}$
	(MeV)	(MeV)	(MeV)	
A,	-39.2	0.6	-38.6	0.030
$A_2$	-39.1	0.6	-38.5	0.030
B <sub>1</sub>	-39.0	0.6	-38.4	0.030
$B_2$	-39.0	0.6	-38.4	0.030

#### TABLE XII.

Values of  $E_{\Lambda}^{(1)}$ ,  $E_{\Lambda}^{(2)}$ ,  $E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$  and  $I_1$  for values of  $\beta_1$  which, minimize  $\left| E_{\Lambda}^{(2)} / E_{\Lambda}^{(1)} \right|$ (BC choice). The  $g_2^{"}$  nucleon-nucleon correlation function, the potential B' and the value  $\varrho=0.121$  nucleons/fm<sup>3</sup> for the density of nuclear matter were used in solving the integrodifferential equation.

Case	${\rm E}^{(1)}_{\rm A}$	E <sup>(2)</sup>	$E_{\Lambda}^{(1)} + E_{\Lambda}^{(2)}$	$\mathbf{I_1}$
	(MeV)	(MeV)	(MeV)	
A <sub>1</sub>	-28.6	0.4	-28.2	0.022
$A_2$	-28.6	0.4	-28.2	0.022
B <sub>1</sub>	-28.5	0.4	-28.1	0.022
$B_2$	-28.5	0.4	-28.1	0.022

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#### ΠΕΡΙΛΗΨΗ

# ΥΠΟΛΟΓΙΣΜΟΙ ΕΠΙ ΤΗΣ ΥΠΕΡΠΥΡΗΝΙΚΗΣ ΥΛΗΣ

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# Μ. Ε. ΓΡΥΠΑΙΟΥ καὶ Β. Κ. ΚΑΡΓΑ

## Σπουδαστήριον Θεωρητικής Φυσικής Πανεπιστημίου Θεσσαλονίκης

Εἰς τὴν ἐργασίαν αὐτὴν ἀναχοινοῦνται ἀποτελέσματα διὰ τὴν ἐνέργειαν συνδέσεως ἑνὸς σωματίου Λ εἰς τὴν πυρηνικὴν ὕλην  $B_{\Lambda}$ , ληφθέντα ἐπὶ τῆ βάσει τῆς διαφορικῆς ἐξισώσεως διὰ τὴν συνάρτησιν ἀλληλοσυσχετίσεως Jastrow, f, διὰ τῆς χρήσεως κεντρικῶν δυναμικῶν καὶ τιμῶν διὰ τὴν πυκνότητα τῆς πυρηνικῆς ὕλης, αἱ ὁποῖαι εἶναι μικρότεραι ἀπὸ τὴν ἀρχικῶς χρησιμοποιηθεῖσαν (0.172 nucleons/fm³) καὶ αἱ ὁποῖαι καθωρίσθησαν μεταγενεστέρως. Δίδονται ἐπίσης ἀποτελέσματα διὰ τῆς χρήσεως τῆς ὁλοκληροδιαφορικῆς ἐξισώσεως διὰ τὴν συνάρτησιν αλληλοσυσχετίσεως χρησιμοποιηθεῖσαν (0.172 nucleons/fm³) καὶ αἱ ὁποῖαι καθωρίσθησαν μεταγενεστέρως. Δίδονται ἐπίσης ἀποτελέσματα διὰ τῆς χρήσεως τῆς ὁλοκληροδιαφορικῆς ἐξισώσεως διὰ τὸν καθορισμὸν τῆς f καθὼς καὶ διαφόρων προσεγγιστικῶν ἐκφράσεων διὰ τὴν συνάρτησιν κατανομῆς σωματίου Λ-νουκλεονίου  $G_{N\Lambda}(r)$  καὶ τὴν συναρτησιακὴν παράγωγον της.